# Introducing Powerwise (PWR): A pairwise and Power Rating method for selecting at-large teams to the NCAA Division I Men's Lacrosse Championship

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**Abstract:** This document describes a new system for selecting teams for the NCAA Men's Division I Lacrosse championship tournament called "Powerwise" that was developed in discussions with the NCAA Lacrosse Selection Criteria and Ranking Committee (SCR). The method is simple, employing hierarchical pairwise comparisons that emphasize on-field performance in head-to-head and common opponent matchups and a simple Massey/Colley/Sagarin-like statistic called the Power Rating (PR) when on-field results are not conclusive. Power Ratings are based on margin of victory and implicitly account for strength of schedule. Powerwise addresses the complexities of team selection in a way that both coaches and fans can understand while improving the fairness, objectivity, and overall quality of the selection process.

**Keywords:** At-large selection; men's Division I lacrosse; pairwise comparisons; Power Ratings; goal differences; on-field results; Sagarin; Massey; Colley.

## 1. Introduction

Four years ago, the lacrosse Selection Criteria and Ranking Committee (abbreviated SCR, herein referred to as the "coaches' committee" or, simply, the "committee") set out to develop a rating system uniquely suited to

select teams for the NCAA Men's Division I lacrosse championship tournament. The committee examined over a dozen potential methods, testing each algorithm against 20 years of data to assess its hypothetical at-large selections.

Drawing on years of committee-member experience, the history of sports ranking, and some of the existing academic literature, the committee identified a variety of desirable factors, including:

- Emphasis on head-to-head and common opponents' records instead of complex analytics.
- II. An unbiased, accurate adjustment for teams' strength of schedule.
- III. The use of margins of victory.
- IV. Minimizing bias and human intervention where possible.
- V. Common-sense results.

The committee dreamed of a method that would re-

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place the existing system for rating teams, which is highly based on the biased and mathematically flawed Ratings Percentage Index (RPI) and closed-door committees that - despite producing reasonable results - feel like a "byzantine black box," leading to a "large amount of speculation, second guessing, and debate each year about [committee] decisions." (Coleman et al. [2010], Colley [2002])

The committee finally settled on a method that integrates a Sagarin-inspired Power Rating<sup>1</sup> (which measures team strength based on goal margins of victory) and a variant of the pairwise comparison method recently used by Division I Hockey. This hybrid method aims to be simpler, more objective, and more transparent than the existing selection process, painting a clearer and fairer picture of which teams deserve to participate in the tournament given their performance in the regular season. This new method is known as "the Powerwise method" or "PWR," reflecting its pairwise and Power Rating components.

This document will clearly and simply describe the Powerwise method and, with luck, convince you of some of its merits, chief among them simplicity, transparency, and common-sense results.

Table 1: Comparison of Popular Methods

Feature	PWR	RPI	Committee	NPI
W/L or Goal diffs.	Both	W/L	Both?	W/L
SoS Adjustment	Yes	Yes**	Yes?	Yes
Simple	Yes	Yes	No	No?
Transparent	Yes	Yes	No	Yes
Objective	Yes	Yes	No?	Yes
Consistent	Yes	No	No?	No
Predictive	No*	No	No	No
Weak team penalty	No	Yes	No?	No

<sup>\*</sup>PWR's component Power Ratings are predictive.

#### 2. The Powerwise Method

## 2.1 Simulating matchups with pairwise

Powerwise works by simulating a scenario in which all teams in a division "play" against each other in hy-

pothetical pairwise matches, competing for Powerwise points.

For each matchup, one team "wins" and the other "loses" due to a three-step hierarchical procedure that evaluates, in order of importance: head-to-head results, each team's record against common opponents, and Power Ratings (to be discussed in the next section).

Given a comparison between two hypothetical teams, the Powerwise point is awarded to:

- I. The team with the superior **head-to-head record.** \*Continue to step II only in case of a nonexistent or tied head-to-head record.
- II. The team with the superior record against **common** opponents.<sup>2</sup>

\*Continue to step III only in case of a nonexistent, tied, or singular<sup>3</sup> record against common opponents.

## III. The team with the higher Power Rating.

After all matchups are examined, the teams are sorted from most-to-least deserving of an at-large bid on the basis of Powerwise points. For MD1 Lacrosse, 77 teams play (are compared in) 76 matchups, so the best possible Powerwise record for a given team is 76-0, and the worst is 0-76.

A notable strength of the Powerwise method is that the majority of its pairwise comparisons are determined solely by on-field results in head-to-head and common opponents' games. Analysis of historical lacrosse data (2013-2024) finds just under 60% of Powerwise points would have been awarded based on a superior on-field record. This enviable percentage falls as the number of teams in a division rises (assuming a constant number of games per season).

<sup>\*\*</sup>The RPI SoS adjustment is flawed, see Appendix B.

<sup>&</sup>lt;sup>1</sup>Consult Appendix A for historical context on the development of Powerwise.

<sup>&</sup>lt;sup>2</sup>Powerwise employs percentage win-loss when calculating common opponent records. One downside of this approach is that it risks downplaying repeated losses. This limitation is discussed in greater detail in Section 4.

<sup>&</sup>lt;sup>3</sup>The suggested Powerwise method optionally ignores any singular common opponent record, on the basis that the results of one game are likely tantamount to randomness. This "ad hoc" adjustment trades simplicity for a little more resistance to chance.

<sup>&</sup>lt;sup>4</sup>Appendix E presents an example Powerwise comparison. Appendix C presents an example ranking list.

Table 2: Percentage of Powerwise comparisons determined by H2H and CO results

Season	2013	2014	 2023	2024	Avg.*
% H2H decisive % CO decisive			17.6 45.2	17.8 45.1	≈19%   ≈53%

\*Avg. Decisiveness of on-field (H2H or CO) = 58.6%

## 2.2 Calculating Power Ratings

As mentioned, in Powerwise matchups where on-field results are indecisive, Power Ratings break the tie.

Powerwise's Power Rating (PR) system is based on goal differentials and designed to estimate the average margin of victory between two teams on a neutral field. The formula is a bit mathematical for a general audience, but it's simpler than it looks.<sup>5</sup>

$$\sum_{i=0}^{n} \sum_{j=0}^{m} (PR_i - PR_j) = \sum_{i=0}^{n} \sum_{j=0}^{m} (score_i - score_j) \pm hfa$$
(1)

Essentially, calculating PRs involves solving a large system of nonlinear equations based strictly on game scores and an adjustment for the home-field advantage, iterating until the average difference between two teams' Power Ratings is equal to the expected (or real) difference in scores were those two teams to play, adjusting for the home-field advantage.<sup>6</sup>

Power Ratings implicitly account for strength of schedule thanks to the inclusion of goal differentials. To enable the use of goal differentials, PRs employ an adjustment to measured score data intended to disincentivize "running up the score." This merits further discussion.

#### 2.2.1 On running up the score

Landmark studies conducted by Barrow et al. and Annis and Craig show that score differential-based methods tend to be both more predictive and more likely to

converge on an interpretable solution than those that use only win-loss data. (Annis and Craig [2005], Barrow et al. [2013])

While it might be unsurprising that the information contained in scores improves ratings, many methods still exclude score data, including Wesley Colley's Colley Matrix. Colley justifies his use of win-loss ratios as a means to "keep it simple," explaining that he didn't want his method to require "ad hoc adjustments" to adjust for "runaway scores." Colley [2002]

Placing emphasis on simplicity is commendable but simplicity shouldn't be bought at the expense of accuracy. NCAA lacrosse teams play far too few games per season—analysts just can't afford to throw out valuable information. Powerwise is designed to use as few "ad hoc" adjustments as possible to enable the use of information-dense goal differentials while minimizing the risk of poor sportsmanship—i.e., incentives to run up huge scores against lesser opponents.<sup>7</sup>

The ad hoc adjustment employed by this version of Powerwise places a "cap" on measured margins of victory at +7 or -7 goals. Any real-world goal that exceeds this limit is disregarded for the purposes of rankings. The number 7 was picked intuitively and may be adjusted by the committee as needed or for other sports. 8

#### **2.2.2** "Why not the RPI?"

The closest analogue to Powerwise is the pairwise ranking system used by the NCAA Men's Division I Hockey committee, which uses an ancient method called the RPI in place of Powerwise's Power Ratings. The RPI is famously problematic, not least because its win-loss methodology produces a systematic bias against midmajor and small conferences. Other problems with the RPI are detailed in Appendix B, including proof of a hypersensitivity to inconsequential results.

 $<sup>^5</sup>PR_i - PR_j$  = difference in estimated Power Ratings;  $score_i - score_j$  = real difference in scores; hfa = home-field advantage  $^6$ Two ways to account for the home-field advantage include a constant adjustment across all teams in a division (determined by historical data or by some other means) or a team-by-team measure that accounts for the fact that different fields (say, Denver's mile-high stadium) perform differently. We opt for the simpler division-by-division average to simplify this analysis, but the preferred method is up for debate.

<sup>&</sup>lt;sup>7</sup>In 2001, famously, the Bowl Championship Series instructed its computer rankers to do away with statistics that measure goal differences altogether or to implement an ad hoc adjustment limiting score margins to plus-or-minus 21 in their code. Powerwise employs a similar adjustment.

<sup>&</sup>lt;sup>8</sup>An alternative method potentially applicable to future iterations of Powerwise involves normalizing goal differential data by taking the "nth" root with n being, for instance, some well-known normalizing constant. Once normalized, additional goals would be subject to diminishing returns.

## 3. Powerwise vs. Historical At-Large Picks

#### 3.1 Data

Official at-large and automatic qualifier data are pulled from the official NCAA websites (NCAA selection committee) and other readily-available sources.

Game-level data come from laxpower.com (historical) and laxnumbers.com (more recent) and are processed to generate ranking lists for each method and the following analysis.

## 3.2 Discrepancies

Differences between historical selections and hypothetical Powerwise picks<sup>9</sup> are presented in Table 3 and include:

- In 2022, Powerwise prefers Notre Dame and Duke to committee picks of Cornell and Brown.
- In 2019, Powerwise prefers Cornell and Denver to Notre Dame and Johns Hopkins.
- In 2018, Powerwise prefers Rutgers, Penn State and Bucknell to Syracuse, UVA, and Villanova.

Table 3: Powerwise vs. Official At-Large Picks (2013-2024, excluding years w/o discrepancies)

Season	Powerwise picks	Official picks
2022	NOD, DUK	COR, BRO
2019	COR, DEN	NOD, JHU
2018	RUT, PSU, BUK	SYR, UVA, VIL
2017	DUK	UNC
2016	VIL, STB	JHU, NAV
2015	COR, HOF	OSU, BRO
2014	YAL	HAR

In '23 and '24 Powerwise agrees with the committee other than in shuffling some seeding. The small number of discrepancies between Powerwise (a purely statistical method) and the committee's expert- and RPI-informed approach might be surprising considering that "bubble" teams (those on the cusp of receiving an atlarge bid) are often extraordinarily well-matched in a crowded field.

That being said, while there is no "holy grail" against which to compare Powerwise and historical at-large

picks, there are good reasons to believe that Powerwise produces common sense ranking lists and potentially even selects teams that show stronger performance against tougher regular-season opponents than those selected by the current method.

At the least, our analysis shows that Powerwise is much better suited to aid the tournament selection committee than the RPI.

## 3.2.1 Quantitative improvements

In-depth statistical analysis is outside the scope of this introductory look at Powerwise, but an analysis inspired by Stocks-Smith's 2021 overview of their College Basketball Rating (CBR) is presented in Appendix F. Stocks-Smith [2021]

Figure F2 plots game scores (y-axis) against opponents' strength as measured by Powerwise (on the x-axis), revealing that Powerwise's picks tended to outperform official picks in the preceding regular season. These results are statistically significant, stand up to the implementation of a goal cap of  $\pm 7$ , and are robust to measuring opponent strength with RPI instead of Powerwise.

#### 3.2.2 Qualitative improvements

Powerwise meets the ideal characteristics set out by the coaches' committee, including mathematical integrity, accuracy, objectivity, simplicity, transparency, consistency, versatility, and sportsmanship (with the caveat that Powerwise's Power Ratings require an ad hoc or asymptotic adjustment to avoid incentivizing running up the score).

The committee method, while admirably accurate given the difficulty of divining (or defining) deservedness of an at-large bid, falls short on simplicity, consistency, and transparency and, when informed by the RPI, appears to be less accurate, less objective, and more prone to biases with respect to Powerwise. 11

<sup>&</sup>lt;sup>9</sup>Appendix C presents 5 years (skipping COVID-19 years) of historical and Powerwise MD1 lacrosse at-large selections.

<sup>&</sup>lt;sup>10</sup>Colley's extremely well-written analysis points out the "treachery" of checking an objective method against subjective truths. Answer-

ing whether a method performs well is remarkably difficult and out of scope for this whitepaper. Colley [2002]

<sup>&</sup>lt;sup>11</sup>Appendix B further details problems we've identified with the RPI. One problem mentioned therein—systematic bias against smaller conferences—is clearly described and analyzed by Paul and Wilson in their 2015 publication. Paul and Wilson [2015]

#### 4. Potential Limitations

Like any method, Powerwise comes with potential complications. The following merit further discussion.

- Power Ratings are adjusted to account for the home-field advantage, but head-to-head and common opponent records are not.
- II. Victory margins—i.e., goal differentials—may connote point spreads or sports gambling.
- III. Powerwise often leads to ties between teams with similar results.
- IV. Percentage win-loss records for common opponent matchups downplay repeated losses.

## Regarding each:

I. Power Ratings are adjusted to account for the homefield advantage, but head-to-head and common opponent records are not.

Should, say, a one-goal spread in a single common opponent game played away determine a Powerwise point? After all, teams tend to overperform at home and underperform in away games. Powerwise elects to ignore the home-field advantage in pairwise comparisons for the sake of simplicity and comprehensibility.

II. Victory margins—i.e., goal differentials—may connote point spreads or sports gambling.

Methods that use game scores (i.e., goal differences or margins of victory) share some terminology with sports gambling—especially the phrase "point spread." Some NCAA sports try to avoid such connotations, especially given the increasing problem sports gambling poses to college campuses. 12

Powerwise puts connotations aside, noting that Vegas/gambling oddsmakers are highly incentivized to pick solid rankings and, for good reason, use margin of victory data in their calculations. The NCAA cannot afford to overlook a method that promises to generate legitimate results, especially considering arguments

like those made by Nick Saban in 2023. 13

III. Powerwise often leads to ties between teams with similar results.

Appendix C displays a full list of Powerwise rankings for the MD1 2024 season. The ratings feature multiple ties between teams that equal numbers of Powerwise points during the pairwise analysis. Though Powerwise might seem less conclusive than other methods that produce fewer ties, the existence of ties amounts to recognizing that many lacrosse teams are so evenly matched that analytics alone are not able to accurately determine which deserves the higher rank. Appendix D resolves this problem by outlining procedures to differentiate between two-, three-, and four- (or more) team ties. <sup>14</sup>

IV. Percentage win-loss records for common opponent matchups downplay repeated losses.

Consider a scenario involving Yale, Princeton, and Canisus. Say Yale loses to Princeton twice in close games and also say that Canisius, a team generally considered weaker than Yale, loses to Princeton only once. Should Canisius win its pairwise comparison against Yale on the basis that Yale has a worse record against their one common opponent?

As-is, Powerwise considers Yale and Canisius' on-field results as equal—0% against their only common opponent. Lacking head-to-head results, the Powerwise point would likely be awarded to Yale based on its bigger Power Rating. An alternative, numeric, win-loss comparison test—i.e., Canisius' record of 0-1 is better than Yale's of 0-2 against Princeton—would reverse this result, potentially altering Yale's end-of-season tournament chances.

Awarding the point to Canisius seems to fly in the face of logic—it's obvious that Yale is the superior team. On the other hand, shouldn't Yale be punished for their additional loss to Princeton? For simplicity's sake and in favor of common sense, Powerwise prefers

<sup>&</sup>lt;sup>12</sup>This is up to the discretion of the relevant NCAA committees, but it's not clear whether avoiding the language associated with point spreads would decrease the incidence of sports gambling—the cat seems well and truly out of the bag.

<sup>13.</sup> When they told me we would be favored against three out of the four teams that got in the playoff, I'm like, why aren't we in the playoffs?"—Nick Saban, in reference to the Las Vegas oddsmakers' picks. Washington [2023]

<sup>&</sup>lt;sup>14</sup>Alternative tie-breakers may be suggested as part of the Powerwise adoption process for different sports.

percentages over numeric records, deferring to Power Ratings slightly more often.

## 5. Conclusions or "Why Adopt Powerwise?"

Powerwise has been rigorously developed, tested, and reviewed to fit lacrosse's unique competitive environment. Substituting Powerwise for the current system of picking at-large candidates for the NCAA Men's Division I lacrosse championship tournament would produce the following results:

- I. Increased trust from fans, coaches, and players in the post-season selection process as a result of increased simplicity and transparency.
- II. Increased acceptance (to the extent possible) of tournament selection decisions thanks to Powerwise's common-sense approach.
- III. Satisfaction from the greater lacrosse community that Powerwise's only metric of success is winning games (and doing so convincingly). Under Powerwise, each team controls its destiny on the field.
- IV. Peace of mind for the selection committee once the flawed, win-loss-based RPI is swapped for the simple, goal differential-based Power Rating statistic. PRs will improve the quality and consistency of at-large picks and the likelihood of rating convergence.
- V. Gratefulness on the part of teams from smaller/weaker conferences that would enjoy a (higher) fair chance of earning an at-large berth because Powerwise avoids the biased RPI strength of schedule calculation.

In conclusion, while most methods focus on predictive accuracy, overstating their ability to rank and forecast in an environment featuring sparse data and human biases, Powerwise places more emphasis on other criteria, including simplicity, fairness, transparency, and ensuring that each fan, player, and coach feels that their favorite team controls its destiny on the field.

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## **Appendix A: Historical Background**

Two individuals served as inspiration in the development of Powerwise. They are Arpad Elo, a Hungarian-American physics professor, and Jeff Sagarin, an MIT statistician.

The Elo system was developed by Arpad Elo in 1939 for the purpose of rating chess players. It functions a bit differently to Powerwise, but at its core, Elo involves inferring performance from wins, losses, and draws against players of varying strengths, i.e., of varying Elo ratings. The difference in Elo scores between two players is interpretable as an estimate (probabilistic) of the multi-game score should they play. In developing Powerwise, its creators were inspired by both the interpretability of Elo ratings and the strength of the idea that underlies it: pairwise comparisons.

Jeff Sagarin, a graduate MIT statistician, is recognized for bringing Power Ratings to the forefront of many sports, including football and basketball. His results appeared in USA Today from the 1980s until recently and were employed by the NCAA Men's Division I basketball championship tournament committee. His method was one of eight used for the college football Bowl Championship Series (BCS) from 1998 to 2014. When the committee eliminated point margins, Sagarin developed a second method without point spreads which remained in use by the BCS.

His algorithm has never been publicly revealed, but it is known that Sagarin used a constant home-field advantage for football and basketball—for instance, 3 or more points, depending on the sport—and introduced cut-offs on margins of victory to discourage running up the score.

Since Sagarin Power Ratings produce "point spreads" and ranking lists that tend to be transitive, many gamblers use them to try to "beat the odds" set by oddsmakers. It is probably for this reason that Sagarin's ratings have not been embraced by the NCAA, at least publicly.

The Power Rating used by Powerwise was first developed by Dr. Lawrence Feldman for college lacrosse in 1997 (under the name of Laxpower) and wasn't specifically guided by inside knowledge of Sagarin's algorithm. The similarity in hypothetical results suggests that the algorithms are similar in function. Both use a constant home-field advantage and goal margin limit, for instance. Laxpower has been described as "uncannily accurate." website [2018]

It isn't clear which convergence criteria is used in Sagarin's rating algorithm, but Feldman iteratively solves equations for each team simultaneously until the average error for each rating is zero when summing the difference between Power Ratings and real margins of victory.

While pairwise comparisons are unusually powerful, given that college sports ratings are unlike chess ratings in that they are limited to a dataset of one (small) season, additional criteria/metrics are required to achieve convergence. That's where Power Ratings come in handy. Lawrence Feldman stuck Power Ratings into an innovative pairwise method and Powerwise was born.

## **Appendix B: Three Problems With the Ratings Percentage Index**

The Rating Percentage Index (RPI) system for ranking teams in Division I sports, particularly lacrosse, has several flaws that affect its accuracy and reliability. Here are three major deficiencies illustrated by example cases:

## Issue 1: Strength of Schedule (SOS) is Based on Opponent Performance, Not Team Performance

The RPI's SOS calculation reflects the win percentage of a team's opponents rather than how a team performed against those opponents. Here's a hypothetical scenario: Should Hampton (Men's D1 lacrosse), ranked 76th in 2024, be invited to the ACC, scheduled tougher competition, and losing all games by a wide margin, despite its losses, Hampton's RPI would jump from 0.3179 to 0.5053, improving by 38 places due to the stronger schedule alone.

This suggests the RPI is more sensitive to a team's opponents' performance rather than its own, distorting rankings. The formula's reliance on opponent win percentages (OWP) and opponents' opponents win percentages (OOWP) creates a situation wherein a team can artificially rise in the rankings by merely playing tougher competition, regardless of actual performance. Table B1 presents the actual RPI results from the 2024 season. If instead, Hampton was to have played in the ACC with a different schedule, table B2 shows Hampton's RPI improvement in rating and rank, from 0.3179 to 0.5053 or 76th to 38th, despite remaining the same team.

Table 4: Hampton Dilemma: original vs. "ACC-ified" RPI rankings

(a) Original RPI Rankings

(b) Adjusted (ACC) Schedule RPI

RPI Rank	Team Name	RPI	Wins	Losses	RPI Rank	Team Name	RPI	Wins	Losses
70	Mt. St. Mary's	0.3663	1	14	38	Hampton	0.5053	0	13
71	St. Bonaventure	0.3538	1	11	39	Vermont	0.4907	8	8
72	Wagner	0.3468	1	12	40	Drexel	0.4883	5	9
73	Queens	0.3353	2	11	41	Air Force	0.4876	9	6
74	Mass-Lowell	0.3350	0	12	42	Quinnipiac	0.4874	9	5
75	Lindenwood	0.3235	0	12	43	Brown	0.4790	3	11
76	Hampton	0.3179	0	13	44	· LIU	0.4730	10	4

*Note.* Hampton ranked 76th during the 2024 season. When its schedule is "ACC-ified," the same roster jumps to an RPI of 38.

## **Issue 2: Ignoring Goal Differentials Invites Inaccuracy**

The second major issue is that RPI only accounts for wins and losses, disregarding the margin of victory or defeat. Consider Team A (which defeats teams by large margins) versus Team B (which wins against the same teams by narrow margins). The RPI system would rate both teams similarly, despite Team A's superior performance. This overlooks the fact that a decisive win (e.g., 15-0) indicates a stronger team than a close win (e.g., 13-12). The absence of goal differential data reduces the granularity of the analysis and leads to less accurate rankings. This approach is mathematically questionable, as it ignores key performance metrics that better reflect a team's strength.

## **Issue 3: Hypersensitivity to Irrelevant Games**

The RPI's sensitivity to small changes in irrelevant or inconsequential games further compromises its accuracy. The example illustrated in Tables 5 and 6 shows how a remote upset, which has little bearing on tournament qualification, can significantly impact rankings.

The left and right panels of Table 5 present ranking lists based on the same data, except for switching the result of a close game played early in the season between two relatively unimportant teams: Delaware and Lafayette. The right panel of Table 5 shows that the rankings of multiple top-20 teams have shifted despite Lafayette and Delaware

having little direct interaction with the tournament contenders. Such hypersensitivity undermines the sense that teams control their own destiny. Table 6 repeats this experiment with Power Ratings, indicating less sensitivity to similar perturbations in the data. Only one, explainable, ranking change occurs in the right panel.

Table 5: RPI rankings before vs. after a single-game upset (teams whose rank changed are in **bold** 

	Original F	RPI	Perturbed RPI		
Rank	Team	RPI	Team	RPI	
1	Notre Dame	0.7100	Notre Dame	0.7097	
2	Duke	0.6632	Duke	0.6631	
3	Johns Hopkins	0.6520	Johns Hopkins	0.6517	
4	Syracuse	0.6404	Syracuse	0.6381	
5	Virginia	0.6371	Virginia	0.6368	
6	Denver	0.6246	Denver	0.6246	
7	Maryland	0.6223	Maryland	0.6223	
8	Princeton	0.6158	Penn State	0.6157	
9	Penn State	0.6158	Princeton	0.6157	
10	Georgetown	0.6147	Georgetown	0.6146	
11	Penn	0.6044	Cornell	0.6038	
12	Cornell	0.6041	Yale	0.6018	
13	Michigan	0.6019	Penn	0.6018	
14	Yale	0.6017	Michigan	0.5994	
15	St. Joseph's	0.5970	St. Joseph's	0.5967	

As you can see, flipping that one "irrelevant" result between Delaware and Lafayette scrambles teams' RPI-derived ranks—especially around the bubble and even in the top 10. The Power Rating list (follows) sees one adjacent swap.

Table 6: Power Ratings before vs. after the same upset (teams whose rank changed are in **bold** 

	Original P	R	Perturbed PR		
Rank	Team	PR	Team	PR	
1	Notre Dame	99.90	Notre Dame	99.90	
2	Duke	97.51	Duke	97.52	
3	Virginia	97.38	Virginia	97.37	
4	Syracuse	97.02	Syracuse	97.00	
5	Penn State	96.90	Penn State	96.91	
6	Johns Hopkins	96.77	Johns Hopkins	96.77	
7	Princeton	96.46	Princeton	96.47	
8	Georgetown	95.78	Georgetown	95.78	
9	Maryland	95.67	Maryland	95.68	
10	Cornell	95.67	Cornell	95.68	
11	Yale	95.47	Yale	95.49	
12	Denver	95.47	Denver	95.47	
13	Michigan	95.25	Michigan	95.21	
14	Towson	94.80	Army	94.82	
15	Army	94.68	Towson	94.69	

## Conclusion

The aforementioned issues with RPI—its flawed SOS calculation, its disregard for goal differentials, and its hypersensitivity to irrelevant games—compromise its effectiveness as a ranking system. As a result, the RPI fails to provide a true reflection of a team's ability, performance, and undermines the sense that teams control their own destiny. This evidence highlights the need for accurate and sophisticated systems that can incorporate additional data, such as goal differentials, and reduce the impact of arbitrary results. In general, Power Ratings do a better job of representing a team's competitive standing than does the RPI.

# **Appendix C: Additional Tables and Figures**

Table 7: Powerwise ratings for the 2024 season. **Tied ratings** are in bold.

Team	Rating	Team	Rating	Team	Rating	Team	Rating
Notre Dame				Harvard	56.00		20.00
Duke Dame	72.00	Lafayette		Villanova	55.00		19.00
		•				Binghamton	
Virginia		Quinnipiac		Delaware		Bellarmine	18.00
Syracuse	70.00	Sacred Heart	35.00	Richmond	53.00	St Johns	18.00
Johns Hopkins	69.00	Drexel	34.00	Colgate	51.00	Cleveland St	15.00
Penn State	69.00	Air Force	32.00	Loyola	51.00	VMI	13.00
Maryland	68.00	Stony Brook	32.00	Rutgers	51.00	Holy Cross	12.00
Denver	67.00	UMBC	30.00	Boston Univ	50.00	Le Moyne	12.00
Georgetown	67.00	Dartmouth	28.00	Lehigh	50.00	Canisius	11.00
Cornell	66.00	Marquette	28.00	Navy	48.00	Robert Morris	9.00
Princeton	66.00	Hofstra	27.00	Utah	45.00	Detroit Mercy	8.00
Yale	65.00	Monmouth	26.00	Providence	44.00	St Bonaventure	8.00
Michigan	62.00	Hobart	25.00	Bryant	43.00	Mercer	7.00
Army	61.00	Bucknell	24.00	High Point	43.00	Mt St Marys	5.00
Towson	61.00	LIU	23.00	Jacksonville	41.00	Queens	4.00
North Carolina	60.00	Manhattan	21.00	Albany	40.00	Wagner	4.00
Penn	60.00	Marist	21.00	Brown	39.00	UMass-Lowell	2.00
St Joseph's	58.00	Merrimack	21.00	Massachusetts	38.00	Lindenwood	1.00
Ohio State	57.00	Siena	21.00	Fairfield	36.00	Hampton	0.00

*Note:* Ties are ironed-out using the common-sense tie-breaker procedures described in Appendix D.

Table 8: At-Large Picks by Season: Official vs. Powerwise

Season 2024	Season 2023	Season 2022
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#	Official	Powerwise	#	Official	Powerwise	#	Official	Powerwise
1	Notre Dame	Notre Dame	1	Duke	Notre Dame	1	Yale	Virginia
2	Duke	Duke	2	Virginia	Virginia	2	Princeton	Notre Dame†
3	Johns Hopkins	Virginia	3	Notre Dame	Duke	3	Rutgers	Princeton
4	Syracuse	Syracuse	4	Maryland	Cornell	4	Cornell <sup>†</sup>	Rutgers
5	Denver	Johns Hopkins	5	Penn State	Maryland	5	Brown <sup>†</sup>	$Duke^{\dagger}$
6	Virginia	Penn State	6	Johns Hopkins	Penn State	6	Virginia	Yale
7	Maryland	Maryland	7	Cornell	Johns Hopkins	7	Harvard	Harvard
8	Penn State	Denver	8	Yale	Yale			

# Season 2019 Season 2018

# Official	Powerwise	#	Official	Powerwise
1 Duke	Yale	1	Maryland	Yale
2 Virginia	Duke	2	Yale	Duke
3 Yale	Loyola	3	Duke	Maryland
4 Notre Dame <sup>†</sup>	Virginia	4	Notre Dame	Denver
5 Loyola	Syracuse	5	Syracuse <sup>†</sup>	Rutgers†
6 Syracuse	$Cornell^{\dagger}$	6	Denver	Penn State
7 Johns Hopkins <sup>†</sup>	Maryland	7	Virginia†	$Bucknell^{\dagger}$
8 Maryland	$Denver^{\dagger}$	8	Villanova <sup>†</sup>	Notre Dam

*Note:* Italicized teams indicate position changes between Official and Powerwise selections. †Indicates teams that appear in one list but not the other (i.e., selection disagreements).

# **Appendix D: Powerwise Tie-breaker Procedures**

The Powerwise Tie-Breaker Procedure outlined below provides a detailed system for breaking ties between teams with identical Powerwise numbers. The procedure takes a step-by-step approach depending on how many teams are tied and uses: head-to-head results, records against common opponents, and power ratings. Here's a breakdown of the tie-breaker process:

#### Scenario 1: Two teams

Powerwise record against other tied teams	Solution
(1-0), (0-1)	The team that is (1-0) is 1 <sup>st</sup> , the team that is (0-1) is 2 <sup>nd</sup>

#### Scenario 2: Three teams

Powerwise record	Solution
against other tied teams	
(2-0), (1-1), (0-2)	The team that is (2-0) is 1 <sup>st</sup> , the team that is (1-1) is 2 <sup>nd</sup> , the team that is (0-2) is 3 <sup>rd.</sup>
(1-1), (1-1), (1-1)	If all three teams have the same records (1-1), the teams are ordered by their power ratings (highest to lowest).

#### Scenario 3: Four teams

Powerwise record against other tied teams	Solution
	The state of the s
(3-0), (2-1), (1-2), (0-3)	The team that is $(3-0)$ is $1^{st}$ , the team that is $(2-1)$ is $2^{nd}$ , the
	team that is (1-2) is 3 <sup>rd</sup> , the team that is (0-3) is 4 <sup>th</sup> .
(3-0), (1-2), (1-2), (1-2)	The team that is (3-0) is 1 <sup>st</sup> , the remaining teams that are (1-2)
	are resolved by Scenario 2.
(3-0), (3-0), (0-3), (0-3)	The teams that are (3-0) are resolved by Scenario 1 and the
	teams that are (0-3) are resolved by Scenario 1.
(2-1), (2-1), (1-2), (1-2)	The teams that are (2-1) are resolved by Scenario 1 and the
	teams that are (1-2) are resolved by Scenario 1.
(2-1), (2-1), (2-1), (0-3)	The first three teams that are (2-1) are resolved by Scenario 2
	followed by the team that is (0-3).

## Scenario 4: More than four teams.

Powerwise record against other tied teams	Solution s	
	The teams are ordered by their power ratings (highest to lowest).	

Series D1: Tie-breaker procedures for 2, 3, 4, or more teams.

## **Appendix E: An Example Powerwise Scenario**

Consider, as an example, Powerwise matchups for Yale illustrated in Table E1.

- I. Yale is awarded the win over Brown because it went 1-0 against Brown in a head-to-head matchup.
- II. Yale did not play Delaware but had a better record than Delaware in games against common opponents (2-0) versus (1-1). If Delaware had gone (2-0) they both would have tied because the comparison is based on percentage wins.
- III. Yale and Richmond did not meet, nor did they have any common opponents, meaning that the Powerwise point is awarded to Yale due to its higher power rating.

Table E1: Example Powerwise comparisons, Yale

Opponent	Who is the winner?	By Head-to- head?	By Common Opponent?	By Power Rating?
Air Force	Yale		Yale (1–0 vs. 0–1)	
Albany	Yale	Yale		
Army	Yale		Yale (2–0 vs. 0–2)	
Bellarmine	Yale			Yale
Binghamton	Yale		Yale (1–0 vs. 0–1)	
Boston University	Yale	Yale		
Brown	Yale	Yale		
Delaware	Yale		Yale (2–0 vs. 1–1)	
Richmond	Yale			Yale
Wagner	Yale		Yale (2–0 vs. 0–2)	

*Note:* Extending this example to all of Yale's comparisons (for this season), 14 were settled by head-to-heads, 37 by common opponents' games, and 25 were determined by Power Ratings.

## **Appendix F: Statistical Analysis**

The main finding presented in this statistical appendix is presented in Figure F2, namely that aggregating game-level data for all discrepancies in at-large selection between Powerwise's ranking list and the historical record, Powerwise appears to pick teams that are slightly more deserving given their regular season on-field performance—a result that's robust within a 95% confidence interval and holds up to a plus-or-minus 7 goal cap.

Table F1 rejects the null hypothesis, presenting evidence that Powerwise's ranking lists are especially unique around the at-large cutoff or "bubble," and Table F3 report the discrepancies between Powerwise's and historical official at-large tournament selections. Finally, Figures F4 and F5 illustrate that F2's findings hold up across seasons (at least at the high end of the opponent's strength spectrum) and when implementing a goal margin of victory cutoff of 7.

Table F1. Correlation test. Mean Kendall's  $\tau$  ( $\pm$  one-season SD), 10 seasons, for each pair of ranking lists across 10 seasons (2012-2024 minus COVID-19 years). \*\*\* = p < 0.001.

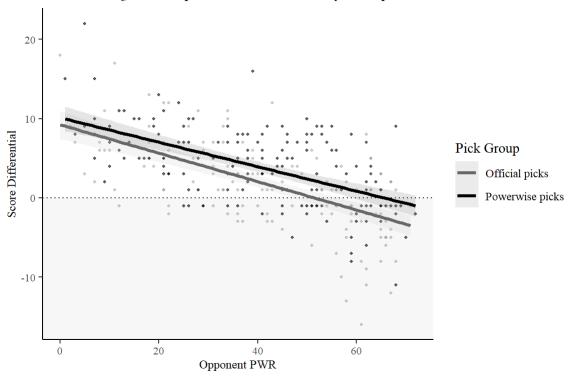
Comparison	$ au~(\pm~{ m SD})$	Signif.
All Teams		
PWR vs. RPI	$0.8566\pm 0.0119$	***
RPI vs. Committee	$0.7630\pm0.1207$	***
PWR vs. Committee	$0.6489 \pm 0.1371$	***
Bubble Teams (Com	$mittee \; Ranks \; 6-16)$	
PWR vs. RPI	$0.7334 \pm 0.1742$	***
RPI vs. Committee	$0.6771 \pm 0.1010$	***
PWR vs. Committee	$0.5723\pm0.0745$	***

**Table F1** presents Kendall's  $\tau$  correlation coefficients comparing Powerwise (PWR), RPI, and Committee rankings across 10 seasons of data (2012-2024 minus COVID-19 years). While PWR and RPI show strong overall correlation ( $\tau$  = 0.8566, p < 0.001), this relationship weakens considerably for bubble teams ranked 6-16 ( $\tau$  = 0.7334, p < 0.001), indicating that Powerwise produces substantively different rankings where it matters most for tournament selection.

**Figure F2** is based on an analysis performed by Stocks-Smith and demonstrates that Powerwise selections outperform official picks by a consistent margin across all opponent strengths (significant at p <  $1.25 \times 10^{-15}$ ). Stocks-Smith [2021] The parallel regression lines indicate this advantage is uniform rather than opponent-dependent, suggesting Powerwise identifies teams with superior overall performance rather than favorable matchup characteristics. This 1-2 goal per game advantage persists across the full range of opponent quality.

Figure F2. Bucketed Score Differential vs Opponent PWR

Shaded bands = 95% CIs; losses shaded; average Powerwise–Official difference is significant at p  $< 1.25 * 10^{-15}$ , driven by intercept.



**Table F3** reveals that across ten seasons, Powerwise and official selections disagreed on 13 at-large bids, with discrepancies ranging from complete agreement (2023-24) to divergence on three selections (2018).

**Figure F4** displays the results of the same calculation shown in F2 for all discrepant years. The shaded confidence intervals indicate the high level of uncertainty associated with a single season's worth of game results. Despite dubious statistical significance at these low sample sizes, Powerwise teams outperform the Official picks in many of the years analyzed, at least against teams at the higher end of the opponent strength spectrum.

Finally, **Figure F5** demonstrates that the results displayed in F2 hold up to measuring opponent strength with the RPI (instead of PWR) and to an adjustment to combat "running up the score," that is, capping the measured goal difference of any given game at plus or minus seven goals.

Table F3. Powerwise vs. Official At-Large Picks by Season

Season	Powerwise picks	Official picks
2022	Notre Dame, Duke	Cornell, Brown
2019	Cornell, Denver	Notre Dame, Johns Hopkins
2018	Rutgers, Penn State, Bucknell	Syracuse, Virginia, Villanova
2017	Duke	North Carolina
2016	Villanova, Stony Brook	Johns Hopkins, Navy
2015	Cornell, Hofstra	Ohio State, Brown
2014	Yale	Harvard

Figure F4. Bucketed Score Differential vs Opponent PWR Across Seven Seasons

Shaded bands = 95% CIs; losses shaded

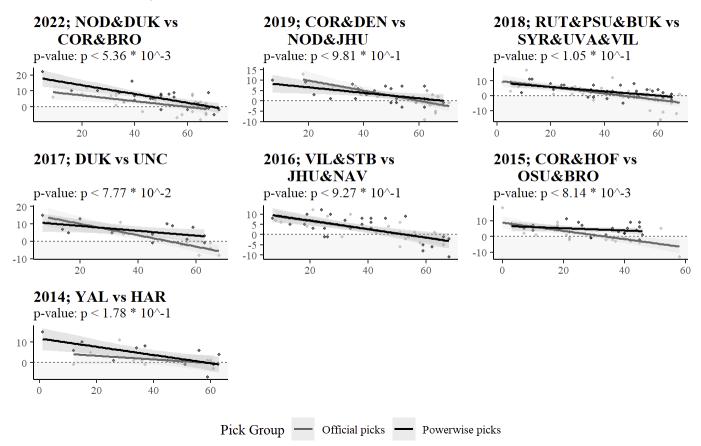


Figure F5. Bucketed Score Differential vs Opponent RPI and PWR (capped ±7)

Shaded bands = 95% CIs; losses shaded

